



Student Name:

Student Number:

**Final Exam, First Semester: 2019/2020**  
**Mechatronics Engineering Department**

**Course Title:** Digital Control  
**Course No:** 0640441  
**Lecturer:** Dr. Jasim Ghaeb

**Date:** 26/01/2020  
**Time:** 2 hours  
**No. of pages:** 5

**Question 1:**

**(7 marks)**

The transfer function of an open-loop control system is given below:

$$G(s) = \frac{2(1 - e^{-5s})}{s(s + 2)}$$

Derive the z-transfer function of the system  $G(z)$ . Assume  $T=1$  sec.

**Question 2:****(9 marks)**

**A-)** The full- scale reference voltage of a 4-bit A/D is 15 V. The analog number comes between two digital levels is truncated to a digital level. Determine:

a-) the maximum quantization error. ( $e_{qmax}$ ).

b-) the maximum analog input signal to A/D without exceeding the quantization error.

**B-)** Find the  $f(k)$  sequence at  $k= 0, 1, 2$  and  $3$  for:

$$F(z) = \frac{z}{z^2 - 0.5z - 0.5}$$

**Question 3:****(7 marks)**

The characteristic equation of the unity f.b system is given below. Use Routh-Hurwitz Criterion to determine the range of (k) for system stability.

$$(8.4 + 0.525k)W^2 + (111.846 - 0.3684k)W + 199 - 0.09013k = 0$$

**Question 4:****(7 marks)**

Use Jury stability test to determine the stability of the digital control system of characteristic equation given below:

$$Q(z) = z^2 - 0.14 = 0$$

**Question 5:****(10 marks)**

A closed-loop system of loop-transfer function of:  $GH(z) = \frac{0.632k z}{(z - 1)(z - 0.368)}$

The Nyquist plot of  $GH(z)$  is shown in Fig.1, which intersects the negative real axis at  $z = -0.231k$ .

1-) Use Nyquist stability criterion to:

a-) determine the maximum value of (k) to keep the system stable.

b-) determine the  $z_{-1}$  for unstable system.

c-) determine the range of (k) for system stability.

2-) If the critical point is taken at (1, j0), what is the value of the angle-traversed for system stability?

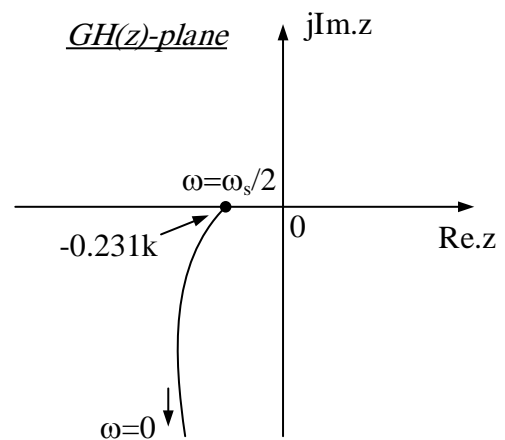


Figure 1